# Principles of Analog In-Circuit Testing 

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In-circuit test (ICT) has been instrumental in identifying manufacturing process defects and component defects on countless varieties of populated printed circuit board (PCB) assemblies for more than 40 years. ICT operates by gaining direct electrical access to the board under test through a bed-of-nails fixture and other limited-access techniques including IEEE 1149.1 boundary-scan and IEEE 1149.8 .1 powered opens. When performing electrical tests, each active and passive component typically is isolated from other surrounding components and tested on an individual basis.

Passive components including resistors, capacitors, inductors, and circuit-protection devices compose the highest percentage of all devices that are populated on today's PCB assemblies. However, the successful isolation and testing of these components during ICT is perhaps the most challenging and the least understood of all modern-day validation practices.

## Measurement Basics

There are two common methods used to measure the resistance, inductance, and capacitance (RLC) of a device. The first is to force an AC current and measure the AC voltage drop across the component. A second method is to force an AC voltage across the component and measure the resultant AC current flowing through the impedance.

Any surrounding components electrically connected to the DUT are neutralized from affecting the measurement by a process known as guarding, which can be either passive or active in nature. In addition, the AC stimulus voltage typically is made low enough in amplitude to avoid accidentally turning on integrated circuit $\mathrm{P}-\mathrm{N}$ junctions that may be attached to the DUT. ${ }^{1}$

The voltage and current measurement data typically is created from a discrete time digitization of the two continuous time waveforms in a phase coherent manner. This results in two data vectors that then are numerically operated upon to extract the impedance value.

The preferred ICT metrology, shown in Figure 1, uses a voltage source as a stimulus generator $\left(\mathrm{V}_{\mathrm{S}}\right)$ and a transimpedance amplifier or a virtual ground current meter to detect the current ( $\mathrm{I}_{\mathrm{X}}$ ) that flows through the unknown device $\left(\mathrm{Z}_{\mathrm{X}}\right)$. The source voltage and device current are both complex numerical values denoted in either Cartesian form ( $V=A+j B$ ) or in polar form $\left(V=|V| e^{j \theta}\right)$.


Figure 1. Simplified DUT Impedance Measurement with Grounded Current Meter
The calculated component impedance is the quotient of the complex voltage impressed across the device divided by the complex device current. Impedance is a complex value that changes as a function of the applied test frequency.

Again, referring to Figure 1, if the op-amp has negligible bias current (IB 0 ) into the negative input terminal, then all of the current flowing through the unknown impedance ( $\mathrm{I}_{\mathrm{x}}$ ) also will flow through the op-amp feedback impedance $Z F$, making $I_{X}$ equal to $I_{F}$. Additionally, the op-amp differential input voltage ( $\mathrm{V}+-\mathrm{V}-$ ) is approximately equal to the output voltage $\mathrm{V}_{\mathrm{o}}$ divided by the op-amp open-loop gain $\mathrm{A}_{\mathrm{vo}}$, which typically is a very large number at lower frequencies.

If the op-amp output voltage is limited to $\pm 10 \mathrm{~V}$ and $\mathrm{A}_{\mathrm{vo}}=2 \times 106 \mathrm{~V} / \mathrm{V}$, then the maximum voltage across ( $\mathrm{V}+-\mathrm{V}-$ ) will be only $\pm 5 \mu \mathrm{~V}$, thereby making the negative input terminal at a virtual ground potential. Finally, the output voltage $\mathrm{V}_{\mathrm{O}}$ and the voltage across the feedback impedance can be described as follows:

$$
\begin{equation*}
V_{O}=-\left[\frac{V_{S} \times Z_{F}}{Z_{X}}\right]=-V_{Z_{F}} \tag{1}
\end{equation*}
$$

Knowing the stimulus voltage amplitude VS, the value of ZF and the voltage VZF across ZF allows you to readily calculate the complex value of the unknown component:

$$
\begin{equation*}
Z_{X}=\frac{\left(\left|V_{S}\right| e^{\beta^{\prime / s}}\right)}{\left(\left|I_{X}\right| e^{\beta^{\prime X X}}\right)}=\frac{\left(\left|V_{S}\right| e^{\beta^{\prime / s}}\right)}{\left(\left|V_{Z_{F}}\right| e^{\beta_{2 g}}\right)} \times Z_{F} \tag{2}
\end{equation*}
$$

where: $\mathrm{V}_{\mathrm{s}}$ and $\theta_{\mathrm{vs}}=$ the respective magnitude and phase
angle of the stimulus voltage
$\mathrm{V}_{\mathrm{ZF}}$ and $\theta Z \mathrm{~F}=$ the respective magnitude and phase angle
of the voltage across the feedback impedance

Calculating the real part of $Z_{x}$ will return the resistive component of the impedance while calculating the imaginary component will yield the inductive or capacitive reactance value. To minimize measurement errors at higher test frequencies, $\mathrm{Z}_{\mathrm{F}}$ also needs to be treated as a complex number.

If the DUT is purely resistive, then the phase information is not required and $Z$ can be replaced with $R$. Equation 2 reduces to:

$$
\begin{equation*}
R_{X}=\left[\frac{V_{S}}{V_{R_{F}}}\right] \times R_{F} \tag{3}
\end{equation*}
$$

Equation 3 can be used to calculate an unknown resistor value by using a DC source voltage rather than an AC stimulus. However, when using DC rather than AC to measure a resistor value, care must be used to minimize any DC offsets and thermal EMFs from relays and dissimilar metal junctions in the stimulus, measurement, and guard paths because they can have a negative impact on the accuracy of the measurement.

## Two- and Three-Terminal Measurements

The circuit configuration in Figure 1 is called a two-terminal or two-wire measurement because only source and measure connections are used. This arrangement rarely occurs on populated PCB assemblies because other components typically are connected to the device being tested. Guarding must be used to eliminate the negative effects of these other components.

Figure 2 shows a simplified circuit where the DUT ( $R_{x}$ ) is connected to other components ( $R_{A}$ and $R_{B}$ ) and indicates how to connect guard terminals to isolate the DUT. For simplicity, these complex impedances now are shown as simple resistances in the figure. Wire terminal resistances $R_{S}, R_{M}$, and $R_{G}$ also are shown. With no passive guard in place at node $G$, a current divider would be created between $R_{x}$ and the series combination of $R_{A}$ and $R_{B}$. As a result, current would flow through both parallel paths and an error in the measurement would occur.


Figure 2. Basic Guarded DUT Impedance Measurement Configuration
With the passive grounded guard $G$ in place, $R_{A}$ now is shunted across the low output impedance source, and $R_{B}$ is placed across the op-amp $V$ - and $V+$ input terminals. With
virtually no voltage present across the V - to $\mathrm{V}+$ terminals, there is negligible current flow through $\mathrm{R}_{\mathrm{B}}$. Virtually all of the current flowing through $\mathrm{R}_{\mathrm{x}}$ also flows through $\mathrm{R}_{\mathrm{F}}$, where the unknown device current is measured with meter $M_{1}$.

## Four- and Six-Terminal Measurements

Path resistances $R_{S}, R_{M}$, and $R_{G}$ can degrade the accuracy of the measurement and may need to be compensated for with additional measurement terminals. For example, if $R_{A}$ is a low-impedance device, then current will flow through it and through the non-zero parasitic guard resistance $R_{G}$. This current will create a voltage at node $G$ that ultimately will force a current through node M and introduce an error in the measurement of the DUT current VRF/RF. The wire resistances $R_{S}$ and $R_{M}$ also will affect the measured value of $R_{X}$. The calculated measurement value of $R_{X}$ that includes the error effects of residuals $R_{S}, R_{M}$, and $\mathrm{R}_{\mathrm{G}}$ for Figure $\mathbf{2}$ is shown in Equation 4:

$$
\begin{align*}
R_{X_{\text {cole }}}=R_{S}+ & R_{M}+R_{X} \times \frac{R_{A} R_{B}+R_{S} R_{B}+R_{M} R_{A}+R_{G}\left(R_{A}+R_{B}\right)}{R_{A} R_{B}+R_{G}\left(R_{A}+R_{B}+R_{X}\right)} \\
& +R_{M} \times \frac{\left(R_{A}+R_{B}+R_{X}\right)}{R_{A} R_{B}+R_{G}\left(R_{A}+R_{B}+R_{X}\right)} \tag{4}
\end{align*}
$$

where: $\mathrm{R}_{\text {xcalc }}=$ the calculated resistance value including measurement errors
$R_{S}=$ the source lead resistance
$R_{M}=$ the measurement lead resistance
$R_{X}=$ the resistance being measured
$R_{G}=$ the guard wire resistance
$\mathrm{R}_{\mathrm{A}}=$ the Thevenin source-side guarded resistance
$R_{B}=$ the Thevenin measurement-side guarded resistance ${ }^{2}$

Minimizing the guard error caused by the finite resistance $R_{G}$ can be achieved by allowing the noninverting terminal of the op-amp input to sense the voltage at node $G$ remotely. This configuration, shown in Figure 3, is what is commonly called a four-wire guarded measurement, not to be confused with a four-wire Kelvin measurement. With the addition of this fourth terminal, there typically will be negligible voltage across $R_{B}$ and therefore negligible error current through $R_{M}$ that would be injected into the transimpedance amplifier from node $G$.


Figure 3. Guarded Measurement Configuration with Guard Voltage Sense

Adding another two terminals or wires can help to eliminate the errors caused by the source and measure wire resistances $R_{S}$ and $R_{M}$. This six-wire metrology is illustrated in Figure 4. Two possible options to connect the op-amp's negative input terminal are represented by the single-pole, double-throw switch. In position $L$, the op-amp current sense terminal is in the local position while the $R$ position denotes a remote sense position. If there is no need for guard terminal(s) or a guard sense terminal, the configuration will reduce to a classic four-wire Kelvin connection scheme that still will help mitigate the source and measure wire losses resulting from $R_{S}$ and $R_{M}$.


Figure 4. Guarded Configuration with Guard Voltage Sense and Remote or Local Feedback

Referring again to Figure 4, the digitizer measurements can be made with two individual meters $M_{1}$ and $M_{2}$ that may have individual gain ( $K_{1}, K_{2}$ ) and offset errors ( $V_{\text {offset1 }}, V_{\text {offset } 2}$ ). These gain and offset terms, even if calibrated out, may drift over time and temperature, negatively affecting the measured value of $R_{X}$ (Equation 5).

$$
\begin{equation*}
R_{X}=\left[\frac{V_{R_{x}} K_{1}+V_{\text {offset }}}{V_{R_{F}} K_{2}+V_{\text {offse } 2}}\right] \times R_{F} \tag{5}
\end{equation*}
$$

However, if a single digitizer is used that is multiplexed between measuring the $R_{X}$ voltage and the $\mathrm{R}_{\mathrm{F}}$ voltage, the gain errors $\mathrm{K}_{1}$ and $\mathrm{K}_{2}$ tend to mathematically cancel because they are nearly the same value. Further, if the real and imaginary terms of the measurement are extracted through a single-bin discrete Fourier transform, then the DC offset terms can be eliminated from the measurement bin. Additionally, the impedance instrument can be designed to interleave alternating measurements of DUT voltage $\mathrm{V}_{\mathrm{RX}}$ and DUT current $\mathrm{V}_{\mathrm{RF}} / \mathrm{RF}$ within a single or multiple AC cycles, thereby adding no additional test time for the unit test period.

A plot of the percentage error as a function of the value of $R_{x}$ for 3 -wire, 4 -wire, and 6 -wire local and remote current sense measurements is illustrated in Figure 5. The conditions for this plot are $R_{S}=R_{M}=0.8 \Omega, R_{G}=0.4 \Omega$, and $R_{A}=R_{B}=50 \Omega$. The error increase of the 3and 4-wire measurements below about $200 \Omega$ is caused by the series resistances $R_{S}$ and $R_{M}$ while the increase in the 3 -wire plot above $200 \Omega$ is a result of the combination of the guard voltage $G$ and a low value of $R_{B}$ that continues to inject error current into the current meter as the current from $R_{x}$ is diminishing with increasing $R_{x}$ values.


Figure 5. Measurement Error vs. Circuit Configuration

## DUT Equivalent Circuits

Most in-circuit testers can return series and parallel equivalent circuits involving $C_{s}, C_{p}, L_{s}$, $L_{p}, R_{S}$, and $R_{p}$ for a given impedance measurement. When measuring a capacitor with no physical series or parallel resistors in the circuit, it is sometimes not clear whether $\mathrm{C}_{\mathrm{s}}$ or $\mathrm{C}_{\mathrm{p}}$ should be used. The calculated values of $\mathrm{C}_{\mathrm{s}}$ and $\mathrm{C}_{\mathrm{p}}$ can be quite different because of the
quality of the component, the measurement path resistance, the component value, and the applied test frequency.

As a general rule of thumb, if the capacitor has a value less than $10 \mathrm{nF}, \mathrm{C}_{\mathrm{p}}$ should be used because the parallel resistance is likely to have a more significant effect on the measurement than the series resistance. Above about 1 to $10 \mu \mathrm{~F}$, the parallel resistance is likely to have less effect than the series resistance, so $\mathrm{C}_{\mathrm{S}}$ should be used in these instances. Similarly, low values of resistance generally should use $R_{S}$ while high values should use $R_{p}$. Comparing the reactance of a capacitor or inductor to the parasitic resistance values can help in determining whether to use a series or a parallel model.

## Other Test Considerations

When testing a component, it may not be clear which pin should be the source node and which pin should be the measurement node. The key to determining the best connections for the test is to consider what else is connected to the pins of the DUT. For example, if one lead of the DUT is connected to a super node such as a power or ground node, this lead should be placed on the source side rather than on the current meter's measurement pin. With a super node, many other nodes will need to be guarded and that will place a lowimpedance and possibly highly capacitive load on the summing junction of the current meter.

A low value resistive load will lower the available loop gain of the amplifier and create a measurement error. A capacitive load will create an open-loop pole in the feedback network and degrade the phase margin of the op-amp and can cause excessive ringing and possible oscillation. In general, any large-value capacitors on a component lead or low-value resistors should be placed on the source node rather than the measure node.

It is possible for a measurement to return a negative value. The most common reason for this is that a large capacitance is being guarded on the measurement node. This guarded capacitor, when combined with the op-amp feedback resistor, creates an open-loop pole in the feedback network, thereby degrading the phase margin of the op-amp. In the closedloop response of the measurement amplifier, there will be amplitude peaking and a large phase change.

If the test frequency is higher than the peaking frequency, then the calculated capacitor or resistor value will likely be negative. Operating at a test frequency below the peaking point or lowering the feedback resistance value should rectify the problem at the expense of some loss in overall measurement accuracy. The approximate peaking frequency is given in Equation 6: ${ }^{3}$

$$
\begin{equation*}
\left.F_{\text {peak }} \approx \sqrt{\left(A_{v o}\right.} F_{P_{1}} F_{P_{2}}\right) \tag{6}
\end{equation*}
$$

where: $\mathrm{F}_{\mathrm{p}} 1=$ open-loop pole of op-amp

$$
\begin{aligned}
& F_{P_{2}}=\frac{1}{2 t} R_{F} C_{G} \\
& \text { Avo }=\text { op-amp DC open-loop gain }
\end{aligned}
$$

## Summary

ICT has been the workhorse of the manufacturing industry for more than 40 years and still is the most economical way to identify the largest range of process and component defects on the manufacturing line. Analog testing of passive components is as important as ever because of their increased usage. Understanding the principles behind analog testing is invaluable in generating stable tests that can hold up to high-volume PCB manufacturing.

## References

1. TestStation Testing Theory, Teradyne, Number 034-324, April, 2006.
2. Khazam, M., "Predicting Test Accuracy for Analog In-Circuit Testing," Proceedings of the International Test Conference, IEEE, 1983, Paper 20.1.
3. Suto, A. J., ACZ High Guard Calculations, GenRad, Application Note, 1996.

## Acknowledgements

Hall, H. P., Multi-Terminal Impedance Measurements, or... Why Do those New Bridges Use So Many Connections?, GenRad, Application Note Form JN 4166A, 1980.

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